

A laboratory volcano (I): application to Kilauea

I) Fire fountain:

kinetic energy is transferred to potential energy (ballistic approximation):

$$\text{velocity} = (2 g H)^{1/2}$$

H: fire fountain height
g: acceleration of gravity

$$H = 400 \text{ m} \quad \longrightarrow \quad \text{velocity} = 100 \text{ m/s}$$



Fire fountain during Puu o'O eruption (Kilauea, Hawaii)



$$\text{gas flux at vent} = \text{velocity} \times \text{surface} = \text{gas volume} / \text{time}$$

$$\longrightarrow \text{gas volume} = \text{velocity} \times \text{surface} \times \text{time}$$

A laboratory volcano (2): application to Kilauea

gas volume at the vent is determined from fire fountain height

perfect gas law:

$$P V = \text{constant}$$

P : pressure;
V: gas volume

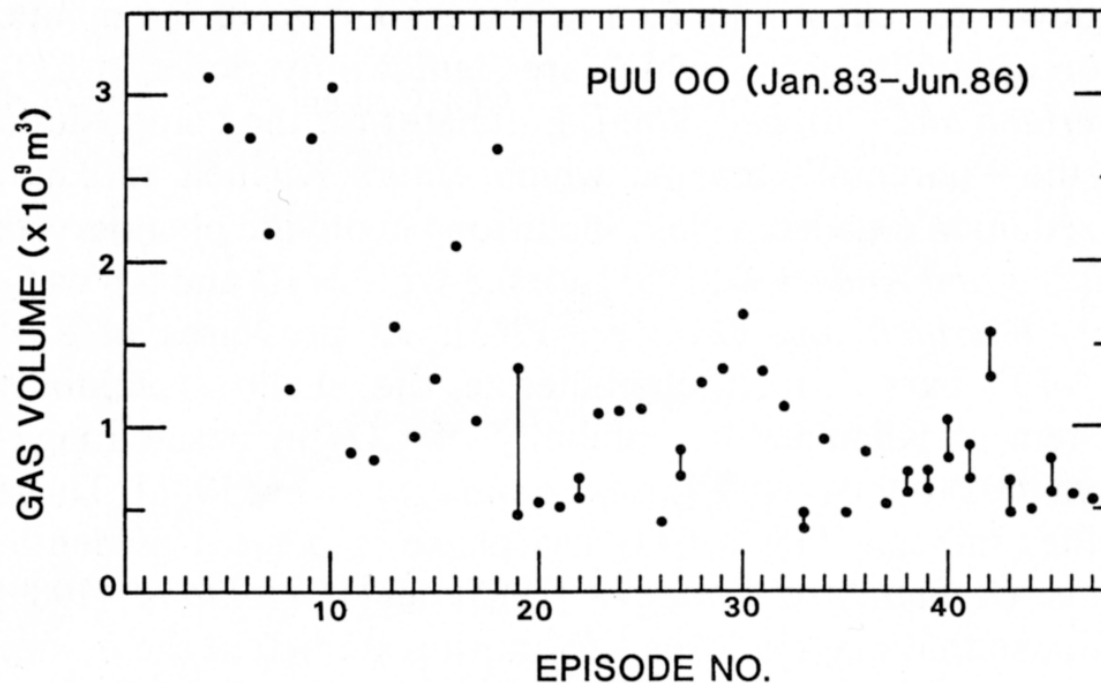


$$P_{g \text{ vent}} V_{g \text{ vent}} = P_{g \text{ reservoir}} V_{g \text{ reservoir}}$$



gas volume in
magma chamber

decrease in gas
volume over the 3
years and a half

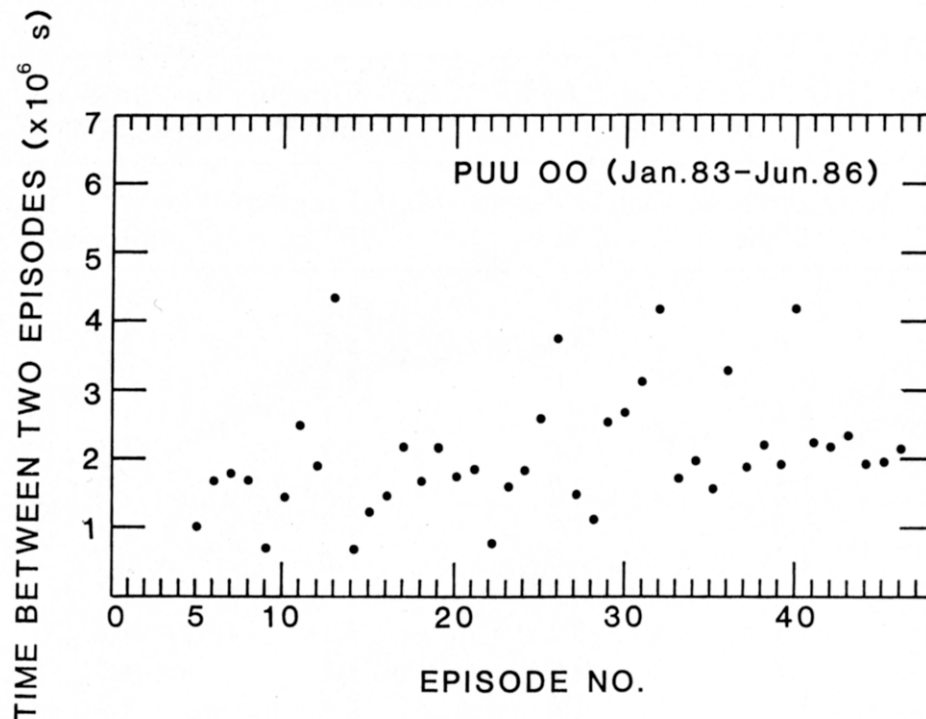


A laboratory volcano (3): application to Kilauea

2) Gas flux in magma chamber Q:

gas volume in magma chamber from fire fountains height

Intermittency between fire fountain: roughly constant



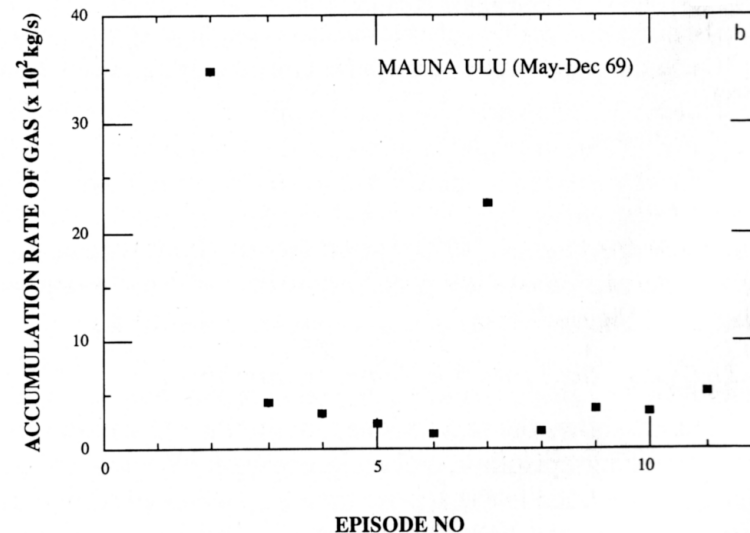
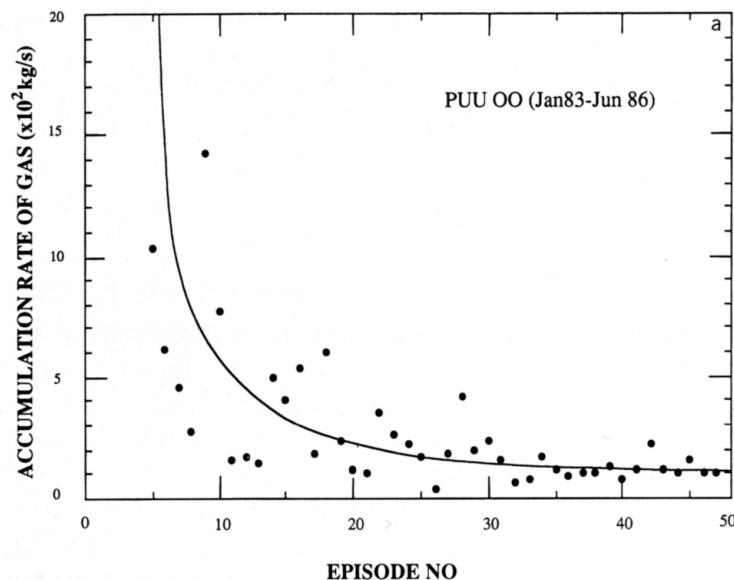
Gas flux in magma chamber is a gas volume at depth over a time during which it has been accumulated

$$Q = \frac{\text{gas volume (2)}}{\text{intermittency (1-2)}}$$

A laboratory volcano (4): application to Kilauea

Gas flux in magma chamber Q :

for Kilauea volcano (Puu O'o and Mauna Ulu eruptions)
calculated for a reservoir at 4 km depth and from fire fountain height



decrease in gas flux in reservoir in time →

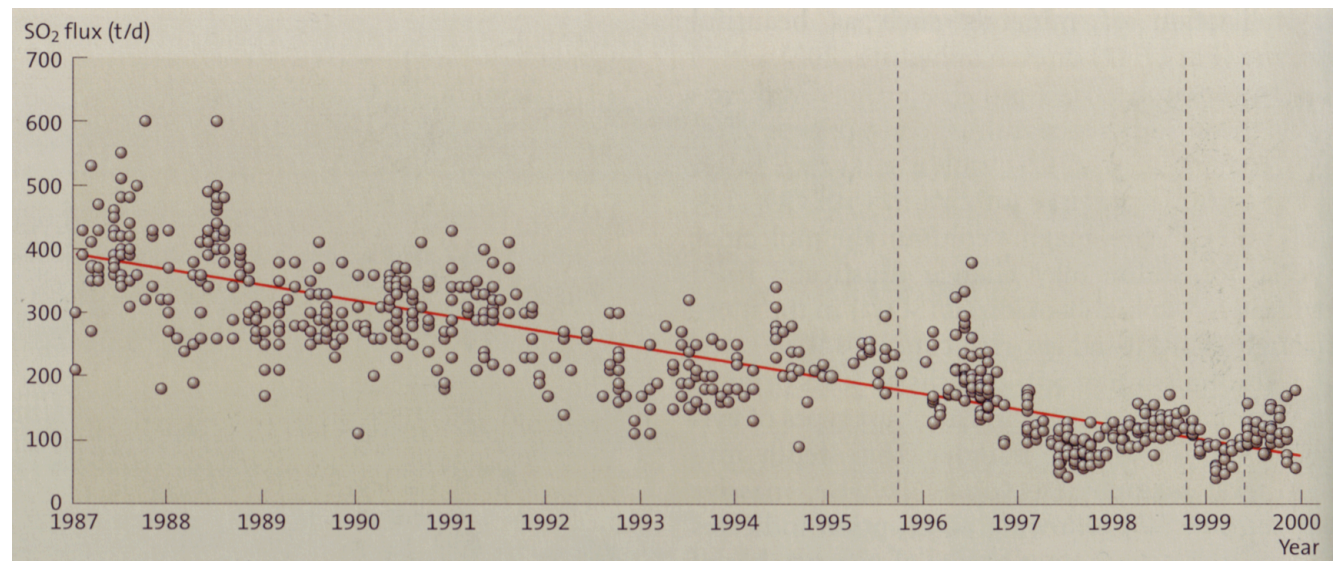
The stopping of fire fountain episodes is associated with the decrease of gas flux in reservoir below the critical gas flux

A laboratory volcano (5): application to Kilauea

The critical gas flux in reservoir, determined from fire fountain height, is approximately 50 kg/s at Kilauea volcano

SO₂ is a magmatic gas which forms at large depth, which may be indicative of the relative evolution of gas volume and gas flux

SO₂ is easily measured at the vent (mass spectrometer: Cospec, FTIR...)

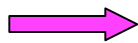
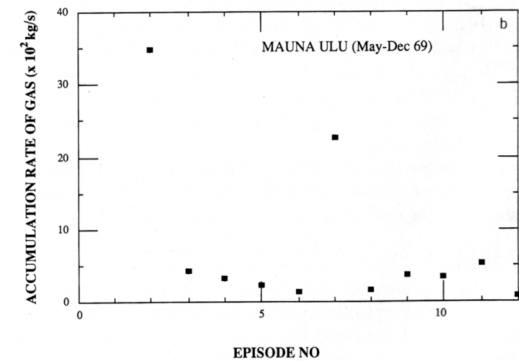
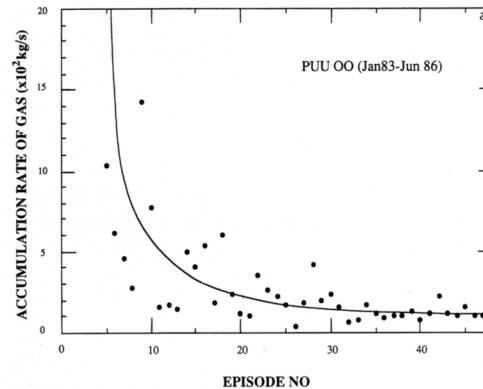


decrease in gas flux during fire fountains is confirmed for the period after the fire fountain episodes (effusive activity)

A laboratory volcano (6): application to Kilauea

Critical gas flux:

estimated from
the fire fountain
height at transition
fire fountain/ effusive



Q_c : critical gas flux: 50 kg/s

$$Q_c = B \frac{\sigma^4}{\rho_{liq}^3 \mu_{liq} d^4} \quad B = f(\epsilon, r_c, r_t)$$



$d = f(\text{critical gas flux})$

Q_c : critical gas flux (m^3/s)
 σ : surface tension ($\text{kg} \cdot \text{s}^{-2}$)
 ρ_{liq} : liquid density ($\text{kg} \cdot \text{m}^{-3}$)
 μ_{liq} : liquid viscosity ($\text{Pa} \cdot \text{s}$)
 d : bubble diameter (m)

ϵ : gas volume fraction
 r_t : reservoir radius (m)
 r_c : conduit radius (m)

A laboratory volcano (7): application to Kilauea

Gas flux in magma chamber Q_g :

from bubble rise velocity v_b : $Q_g = \alpha v_b S$

$$Q_g = \alpha \frac{(1 - \alpha) d^2 (\rho_{liq} - \rho_{gas}) g}{18 \mu} S$$

α : gas volume fraction in reservoir

S : area of magma chamber (m^2)

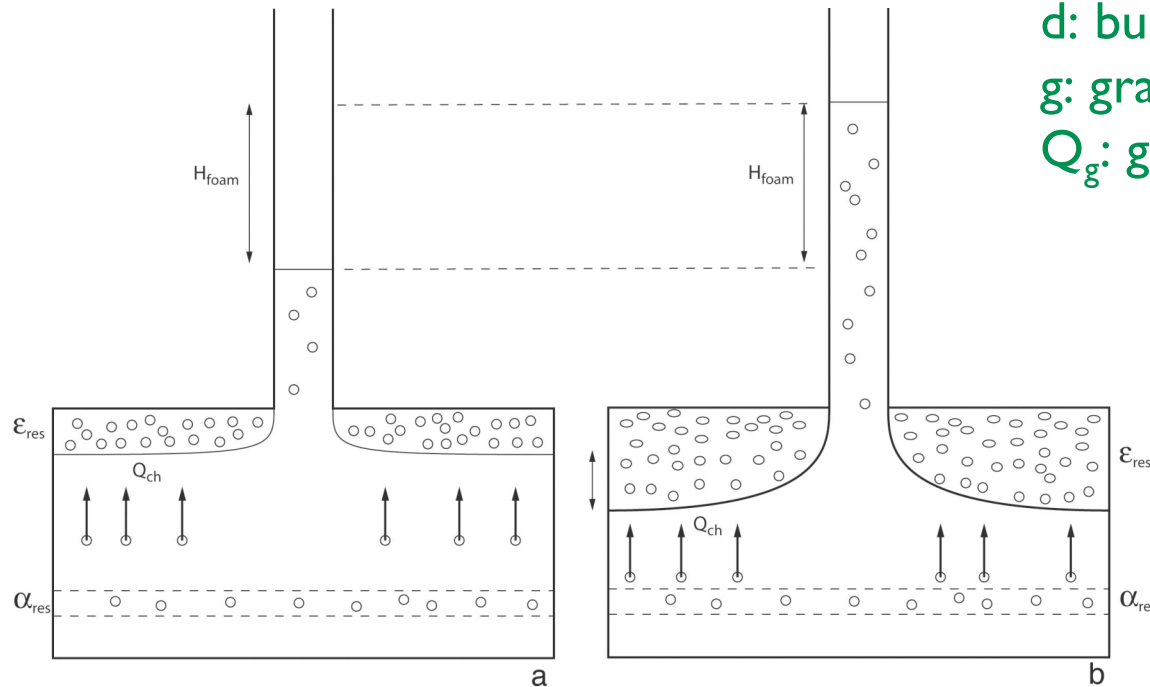
μ : viscosity (Pa.s)

ρ_{liq} : liquid density ($kg.m^{-3}$)

d : bubble diameter (m)

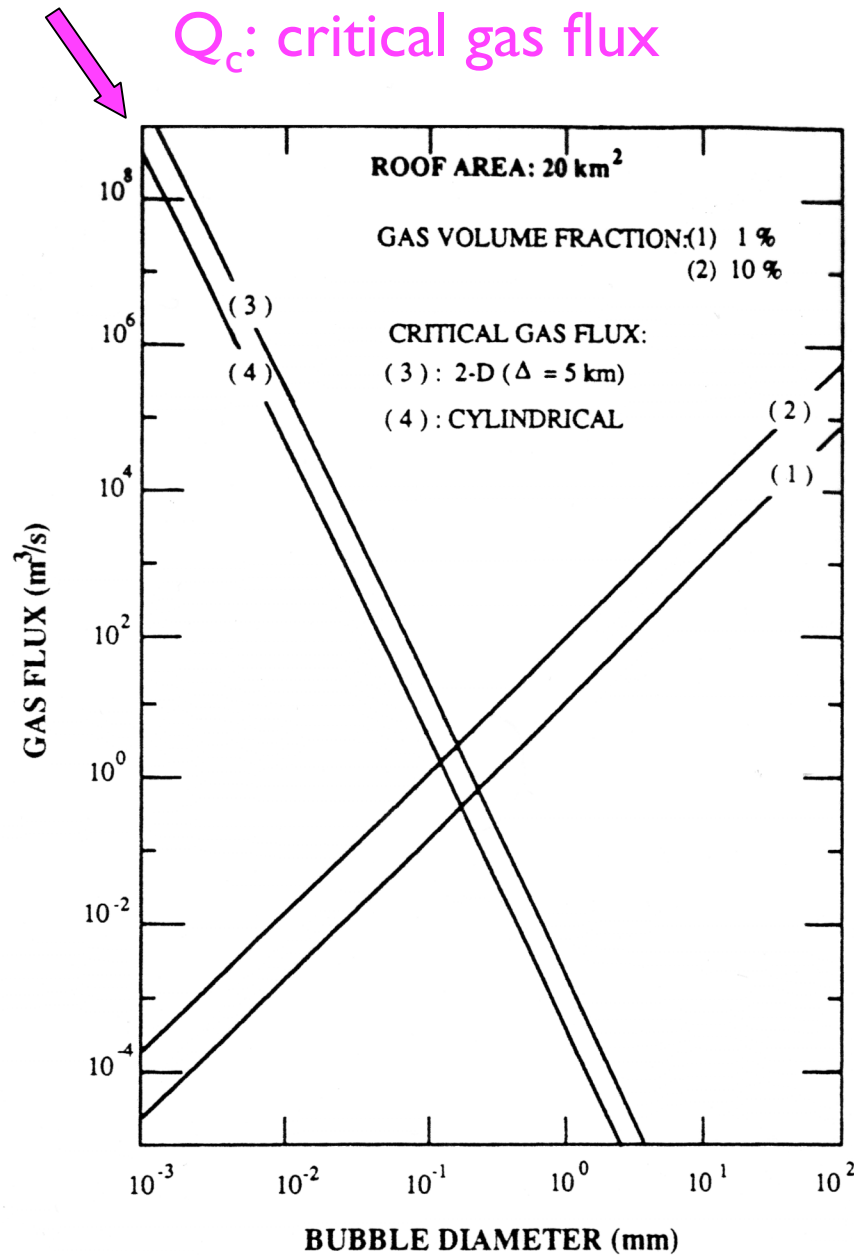
g : gravity

Q_g : gas flux (m^3/s)



gas flux = $f(\alpha, d, \text{area})$

A laboratory volcano (8): application to Kilauea



Etna, 600 m
(Sept 26 1989)

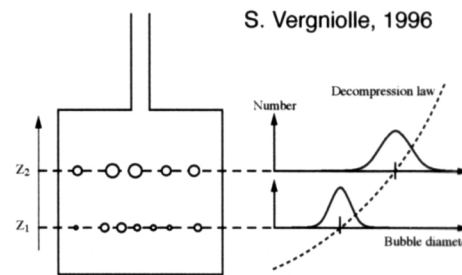
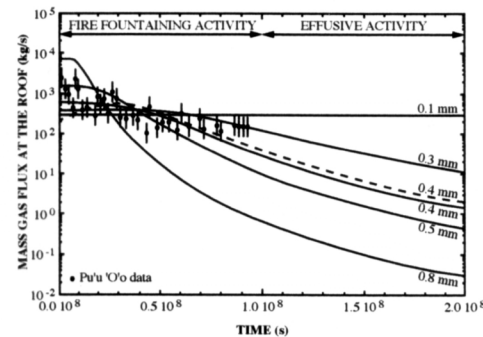


bubble rise

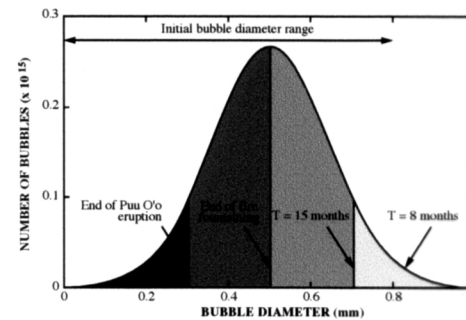
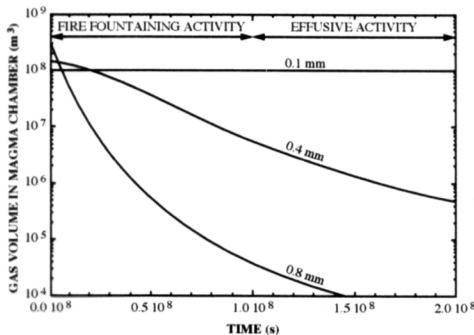
bubble diameter
in magma chamber
0.4 mm

A laboratory volcano (9): application to Kilauea

Duration of an eruption : evolution of a polydisperse suspension of bubbles initially widespread everywhere in a closed magma reservoir



Duration of eruption



time for smallest bubbles to reach the top of the magma chamber

Eruption stops when magma chamber has been depleted of most of its bubble content

A laboratory volcano (10): application to Kilauea

General trend: decrease of gas flux in time

1st bubbles are the largest and the latest bubbles the smallest

2 dimensionless times based on observed durations : τ_f^* and τ_e^*

Duration of fire fountain τ_f :

$$\tau_f^* = \tau_f \frac{d_0^2 (\rho_{\text{liq}} - \rho_{\text{gas}}) g}{18 \mu h_c}$$

$\tau_f^* = 1.1$: Puu O'o eruption (1987-now)

$\tau_f^* = 1.3$: Mauna Ulu eruption (1969-1971)

Duration of eruption τ_e :

$$\tau_e^* = \tau_e \frac{d_0^2 (\rho_{\text{liq}} - \rho_{\text{gas}}) g}{18 \mu h_c}$$

$\tau_e^* = 4.2$: Puu O'o eruption (1987-now)

$\tau_e^* = 4.3$: Mauna Ulu eruption (1969-1971)

Mean bubble diameter: 0.4 mm: Puu O'o and Mauna Ulu eruptions

Degassing layer = 2 km (Puu O'o) and 300 - 500 m (Mauna Ulu)

Duration of Puu O'o eruption is 6 times longer than Mauna Ulu

A laboratory volcano (I I): application to Kilauea

Lava pond, Puu O'o eruption
(Kilauea, March 1988)

Makaopuhi lava lake, 1965:
height = 83 m = h_c
viscosity = 50 Pa.s = μ



Temperature measurements + model of thermal convection

➡ for the first 5 months of emplacement:
no thermal convection because of bubble rise

$\tau_e^* = 5 \text{ months}$
 $\tau_e^* = 4.2$ } mean bubble diameter $d_0 = 1 \text{ mm}$

same order of magnitude as for Puu O'o and Mauna Ulu eruptions

A laboratory volcano (I2): application to Etna (Italy)

Recent activity: a series of regular eruptive episodes
(64 episodes in 2000; 15 episodes in 2001; id 1989; 1998)
each episode: a series of Strombolian explosions
a episode lasts a few hours, intermittency: a few days



Etna,
July 2001
(Pfeiffer)

Each explosion corresponds to large bubble bursting
(diameter of several meters)

Acoustic measurements → gas volume at vent

A laboratory volcano (I3): application to Etna (Italy)

FTIR measurements: gas composition with high CO_2/S and S/Cl

→ violent emptying of a foam layer accumulated at 1.5-2 km depth

Perfect gas law → Gas volume at depth of reservoir

+ intermittency between episodes (3-5 days) → Gas flux at depth of reservoir
Bubble diameter: 0.7 mm

9 May-13 July 2001: trachybasalt
at summit (South East Crater)

17 July-9 August 2001: flank-eruption:
alkali-rich basalt (primitive):
3.4 wt% H_2O ; 0.11-0.41 wt% CO_2 .

Etna, flank eruption 2001



Origin of flank eruptions is not well-known
but in July 2001 associated with new fresh magma

Basaltic magma reservoirs

1. Physical parameters

2. A laboratory volcano:

3. Gas volume measurements

4. Conclusion

Velocity measurements
with a Sodar at
Stromboli, juin 1991



Basaltic magma reservoirs

1. Physical parameters

2. A laboratory volcano:

3. Gas volume measurements

- a) ballistics and radar
- b) acoustic records

4. Conclusion

Velocity measurements with a Sodar at Stromboli, juin 1991



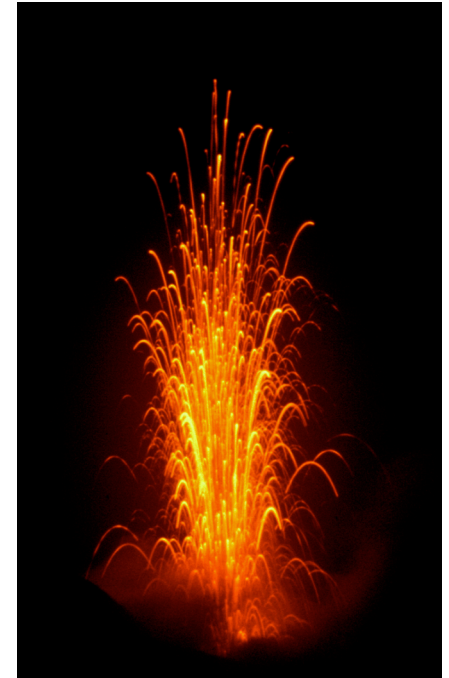
Direct measurements (I): ballistics

Strombolian explosion:

A series of bubbles bursting at
the top of the magma column

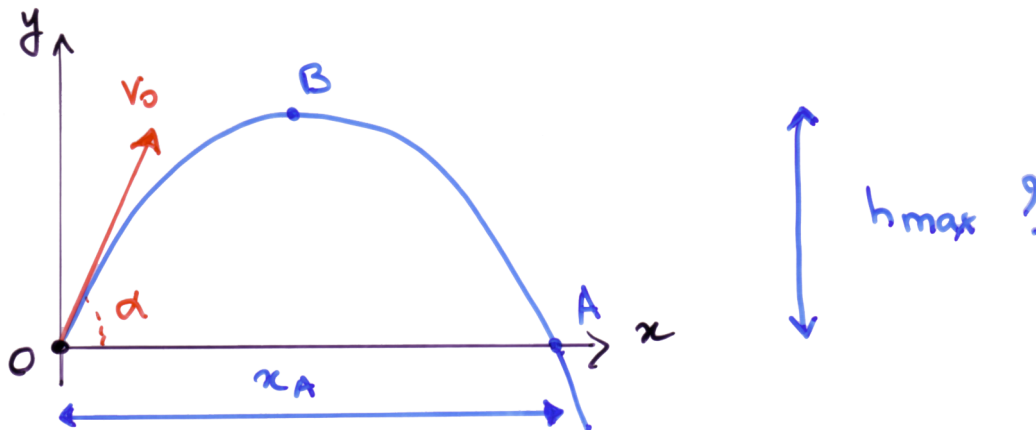
duration: a few seconds

Intermittency: minutes to hours



Ballistic of a point:

Stromboli, 1992



assumption:
no air resistance

$$h_{\max} = \frac{v_0^2 \sin^2(\alpha)}{2g}$$

Direct measurements (2): ballistics

For a vertical gas jet $\longrightarrow v_0 = (2 g h_{\max})^{1/2}$
(kinetic energy is transformed into potential energy)

Example: Stromboli

$$h_{\max} = 100 \text{ m} \longrightarrow v_0 = 50 \text{ m/s}$$

v_0 is not too sensitive to h_{\max} , which is difficult to measure

Impact on the ground: x_a

$$x_a = \frac{v_0^2 \sin(2\alpha)}{2g}$$

x_a is maximum for $\alpha = 45^\circ$

$$\alpha = 60^\circ; v_0 = 50 \text{ m/s}; x_a = 220 \text{ m}$$

Maximum distance reached by ballistics ejecta: a few km.

If a small plume is formed, small ejecta can be carried further away

Direct measurements (3): ballistics

Bubble rise in a magma:

μ : viscosity (Pa.s);

ρ_{liq} and ρ_{gas} liquid and gas density (kg/m³);

$$v_{\text{gas}} = \frac{d^2 (\rho_{\text{liq}} - \rho_{\text{gas}}) g}{18 \mu}$$

balance between viscous resistance in magma and bubble buoyancy

Basalt: a bubble of 1 mm in diameter (d) takes 6 months to rise 1 km

particle in gas jet:

$$v_{\text{part}}^2 = \frac{2 \pi d (\rho_{\text{liq}} - \rho_{\text{gas}}) g}{3 C_d \rho_{\text{air}}}$$

C_d : drag coefficient (turbulent) = 1.18

balance between friction in air and particle weight

Remark: Stromboli; crystal settling: $d = 1 \text{ mm}$; $v_{\text{cryst}} = 56 \text{ m/s}$

Apparent velocity: $w = v_{\text{gas}} - v_{\text{part}}$

ballistics

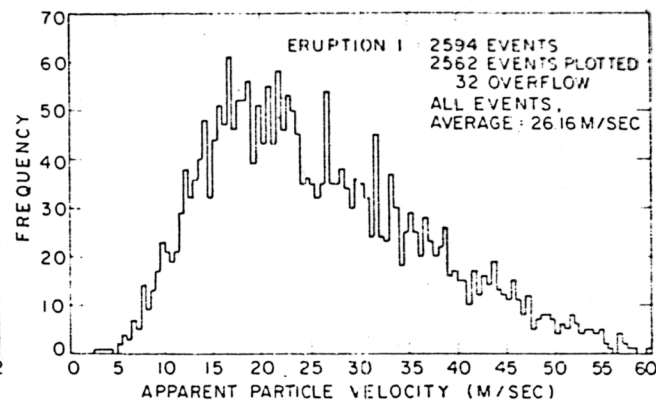
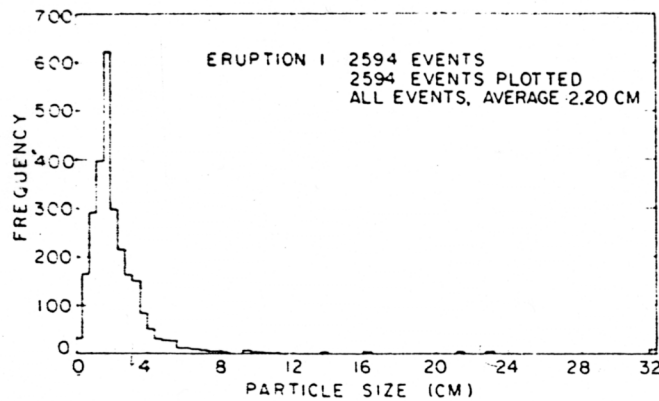
→ $v_{\text{part}} = 50 \text{ m/s}$: particle velocity

→ $v_{\text{gas}} = 100 \text{ m/s}$: gas velocity

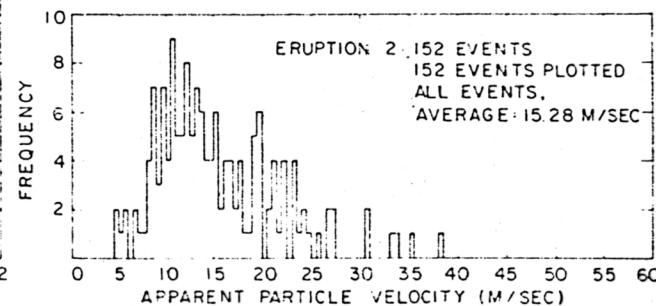
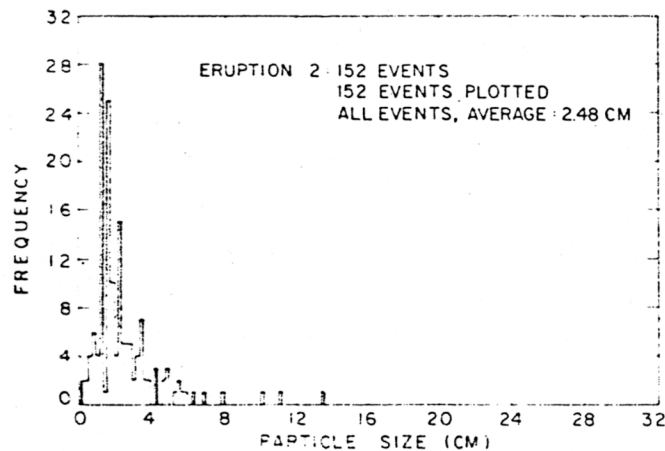
Direct measurements (4): ballistics

Particle diameter (cm)

Apparent Particle velocity



$$w = v_{\text{gas}} - v_{\text{part}}$$

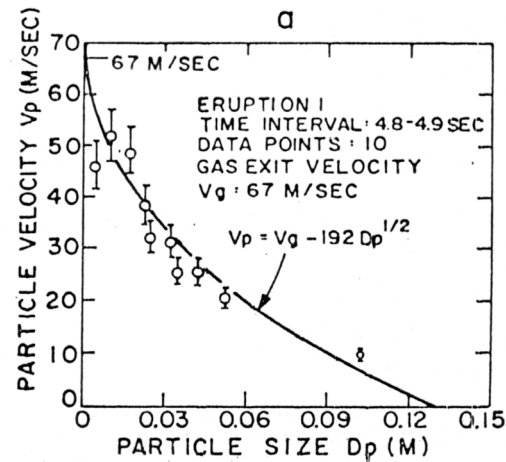


Stromboli,
1971

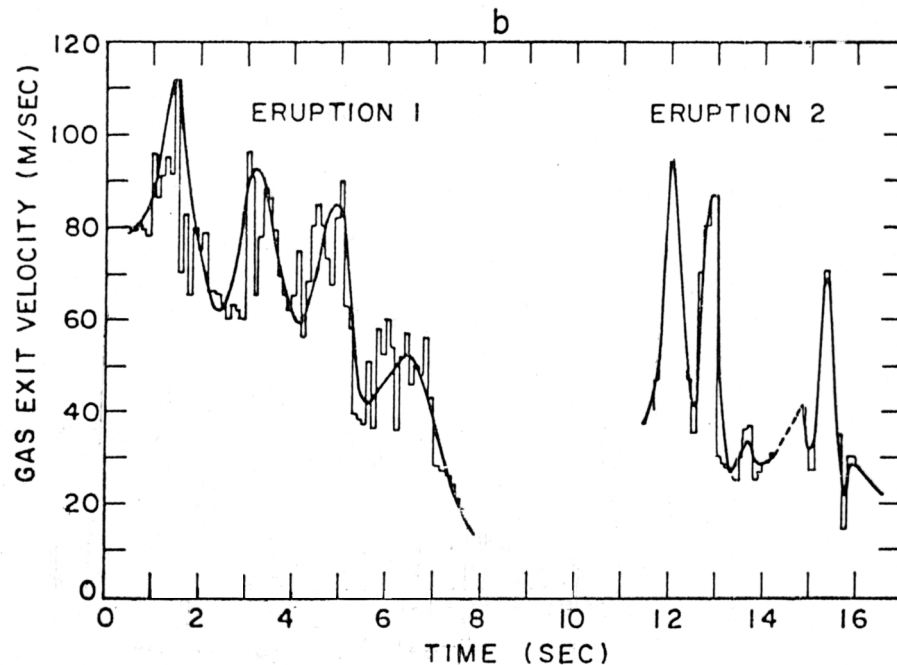
Fig. 9. Frequency distributions of particle sizes and apparent particle velocities for the bulk of the two eruptions studied.

Direct measurements (5): ballistics

Stromboli,
1971

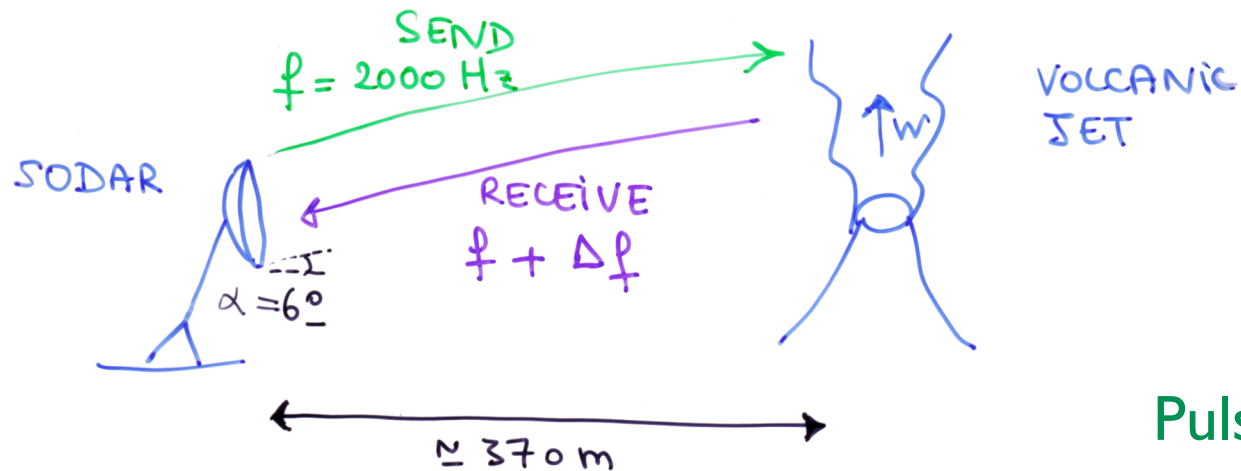


Apparent particle velocity:
the smallest particle moves
at the same velocity as the gas



Oscillations in gas jet:
attributed to resonances
of the conduit
(300 m length)

Direct measurements (6): radar: Acoustic sounder



Doppler shift



velocity

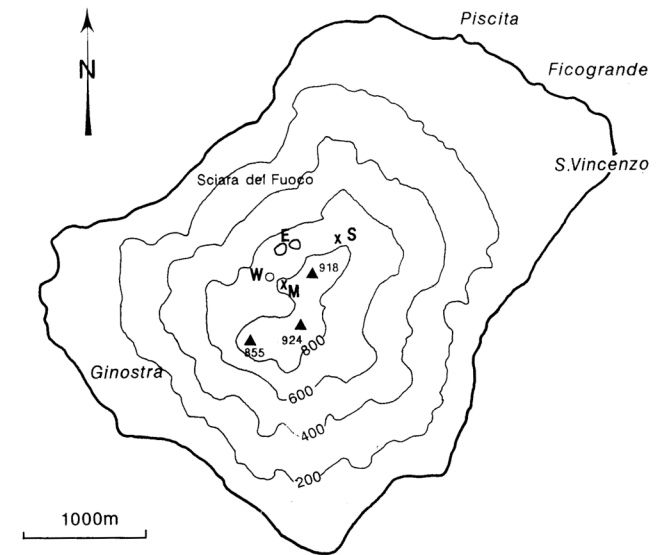
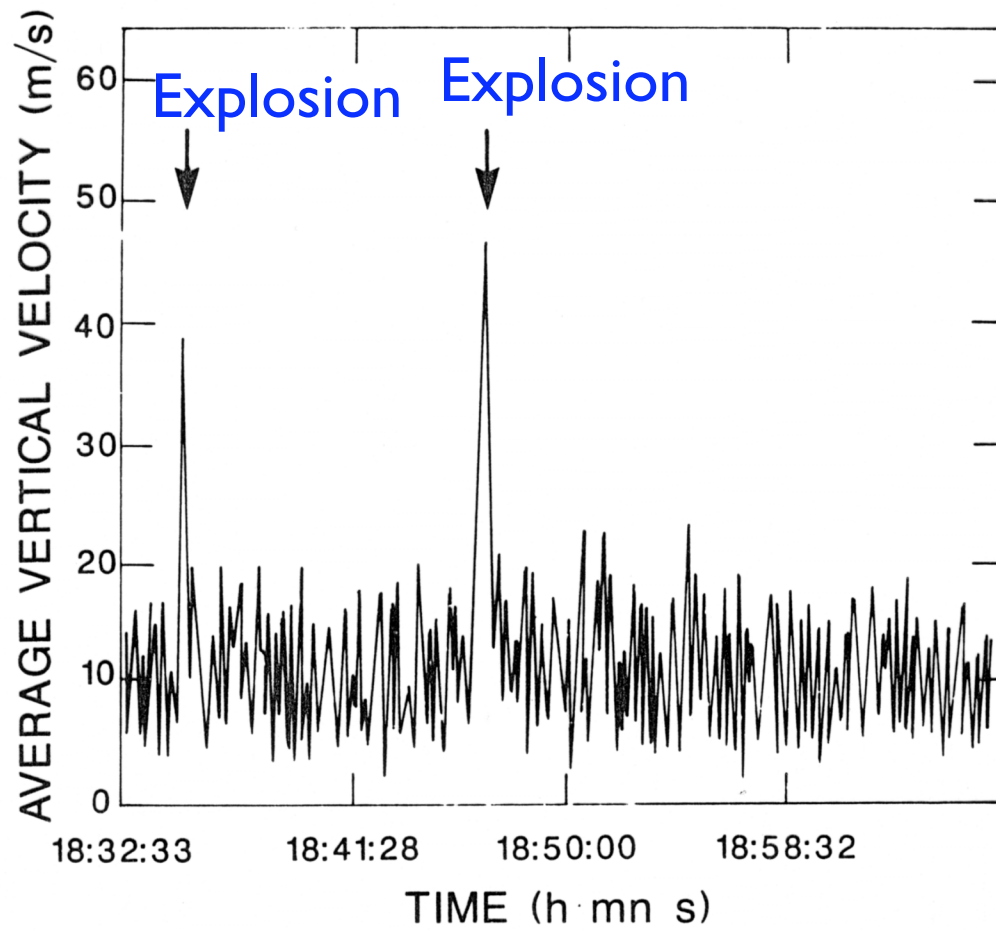
Pulse: each 4 s; $\tau_{\text{on}} = 50 \text{ ms}$

$$\Delta f / f = - 2 w \sin(\alpha) / c$$

c: sound speed
air: 340 m/s
hot gas : 700 m/s

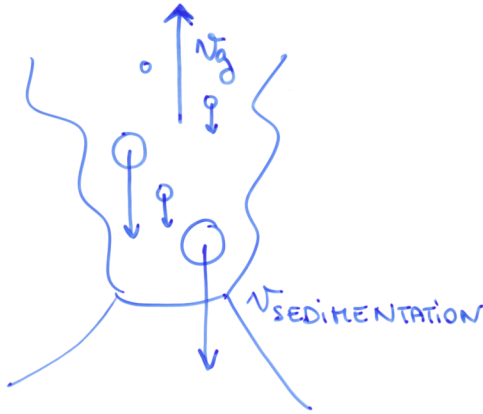


Direct measurements (7): Acoustic sounder



Summit vents
at Stromboli

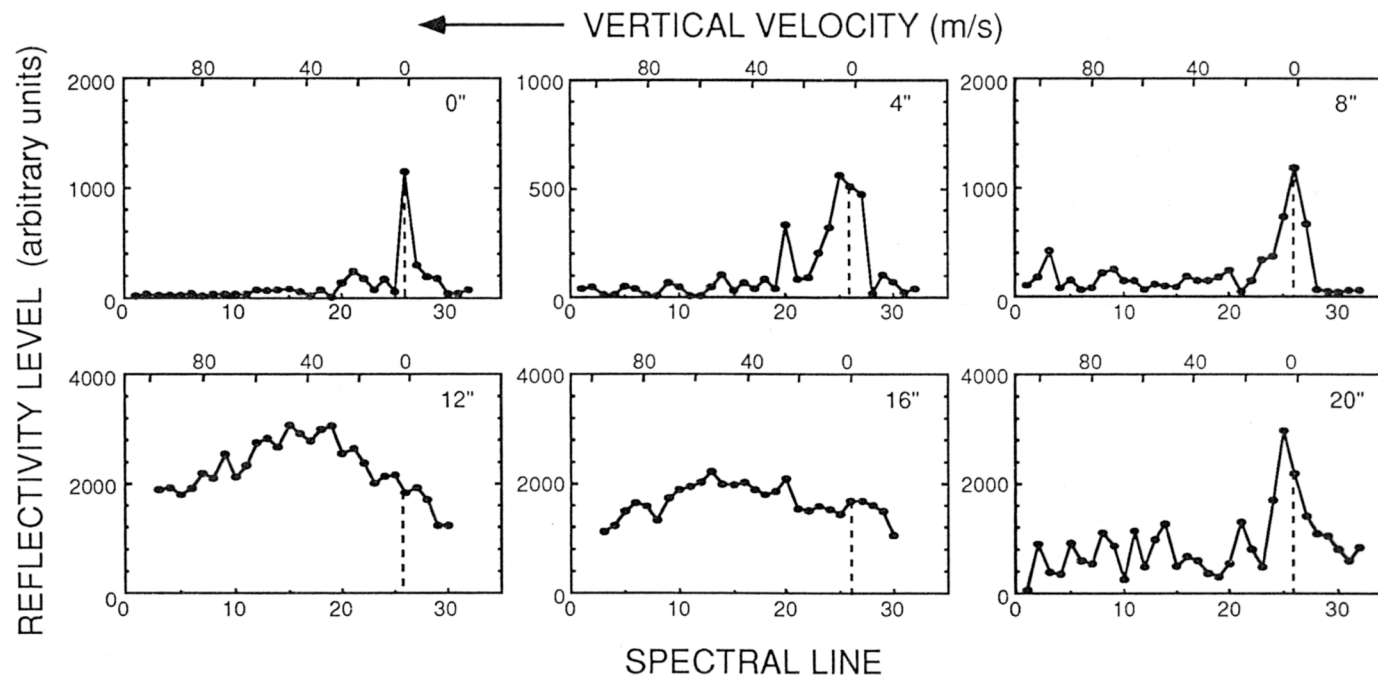
Direct measurements (8): Acoustic sounder



$$w = v_g - v_{\text{part}}$$



A range of particles velocity because
of a range of particle diameter



Basaltic magma reservoirs

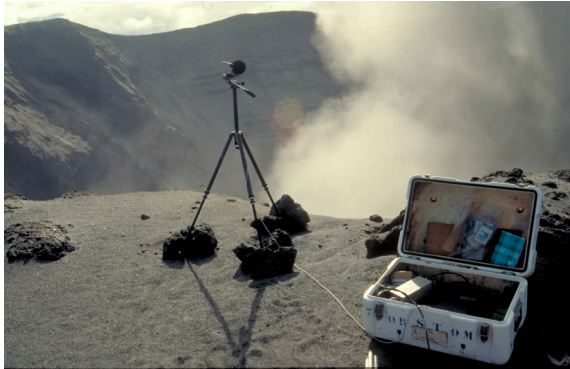
1. Physical parameters
2. A laboratory volcano:
3. Gas volume measurements
 - a) ballistics and radar
 - b) acoustic records
4. Conclusion



Acoustic measurements
at Yasur, Vanuatu, 1993



Direct measurements (9): Acoustic records



Microphone,
Yasur, 1994

Yasur, 1994



Sound is produced by a volcano has a strong intensity

Sound : variation of pressure, which propagate in a compressible fluid
correspond to density variations in an elastic media
radiation of sound in air from volcano vent

Sound waves are longitudinal waves (P):
elements of fluid move parallel to the direction of propagation
move back and forth: zones of compression and dilatation

Acoustic: related to oscillatory motion
 identical to seismology except propagation in air

Direct measurements (9): Acoustic records



Microbarograph
at Yasur
(oct 2002)

Yasur,
(oct 1993)



Sound is produced by a volcano \longrightarrow Informations on volcanic activity
recording sound waves is a way to monitor volcanic activity

What is the source of the sound?

Frequency = size of the source

Amplitude = overpressure

Phase = initial condition



source = gas

ejecta velocity

Evolution in time of the eruption characteristics

Direct measurements (10): Acoustic records

First developed on Strombolian explosions:

permanent activity and not dangerous (close to the vent)

A series of bubbles bursting at the top of the magma column

duration: a few seconds

Intermittency: minutes to hours

Etna,
July 2001
(Pfeiffer)



Ejecta velocity = 50 m/s

Gas velocity = 100 m/s

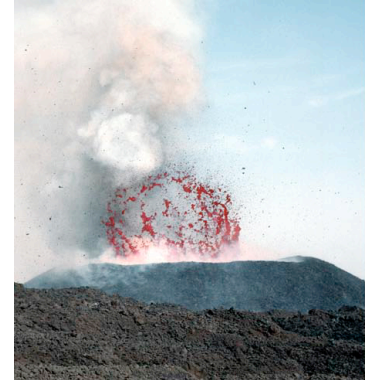
Ejecta size = 2 cm (Stromboli)

= 20 cm (Etna)

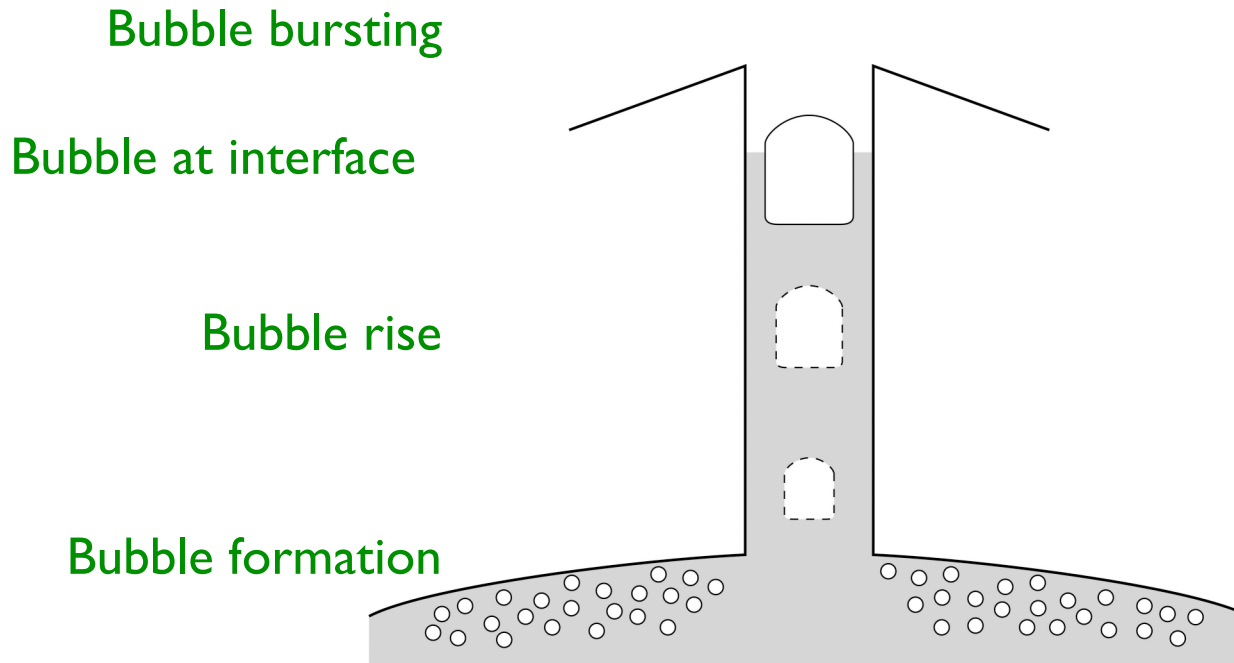
Bubble diameter = several meters (Heimaey, Etna, Erebus, Kilauea...)

Direct measurements (II): Acoustic records

Etna, July 2001



Gas exists in conduit for basaltic eruption:
strombolian explosions: a few meters long
fire fountains: several tens of meters long



sound waves

bubble size and pressure

bubble pressure at depth



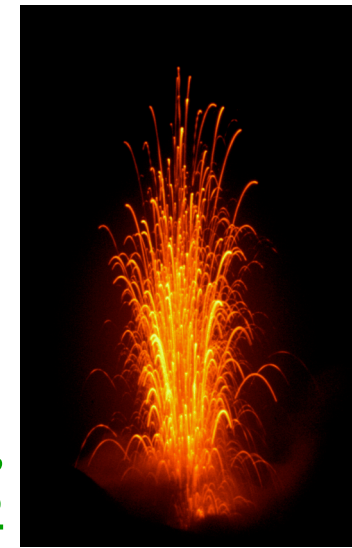
Eruption dynamics

Direct measurements (12): Acoustic records

Strombolian explosions or fire fountains:
origin of large bubbles at depth (carry informations from depth)
understanding large bubbles, is understanding eruptive behaviour



Fire fountain
Puu o'O eruption
(Kilauea, Hawaii)



Stromboli,
1992

Acoustic measurements:
remote measurements of « magmatic » bubbles at the vent

Observations at the surface
+ flow model in conduit → quantitative information at depth

Direct measurements (13): Acoustic records



Bubble bursting at the surface
of lava lake (Kilauea, Hawaii)

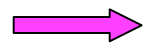
Sound is produced by bubble breaking
at the surface of lava column / lava lake



bubble must have a
residual overpressure

Bubble breaking = balloon bursting ?

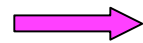
balloon bursting



frequency = sound speed / radius

sound speed = 340 m/s

+ radius = 2 m



frequency = 150 Hz

Frequency measured on volcanoes: 1 - 10 Hz

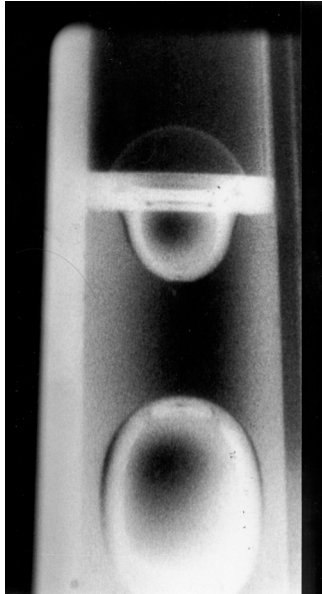


more than 1 order of magnitude discrepancy
the mechanism is not bubble bursting such as for a balloon

Direct measurements (14): Acoustic records

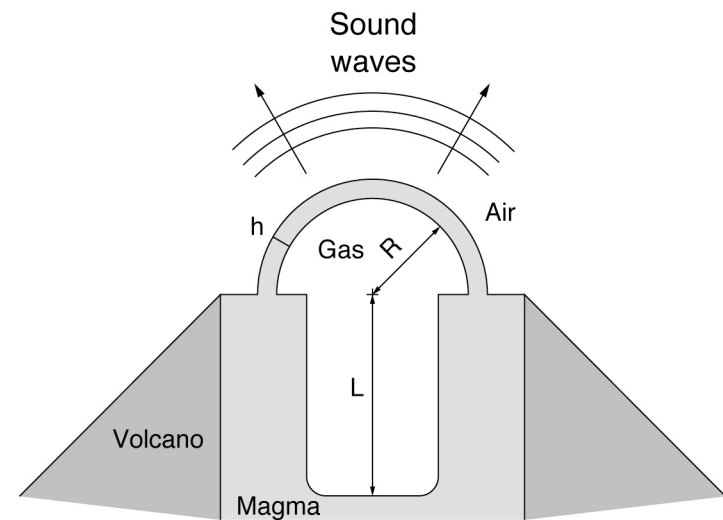
Bubble vibration model:

bubble arrives at the surface of lava column with an overpressure ΔP



Laboratory experiments
(silicone oil 12.5 Pa.s,
tube diameter = 0.14 m)

Sketch of bubble
vibration model

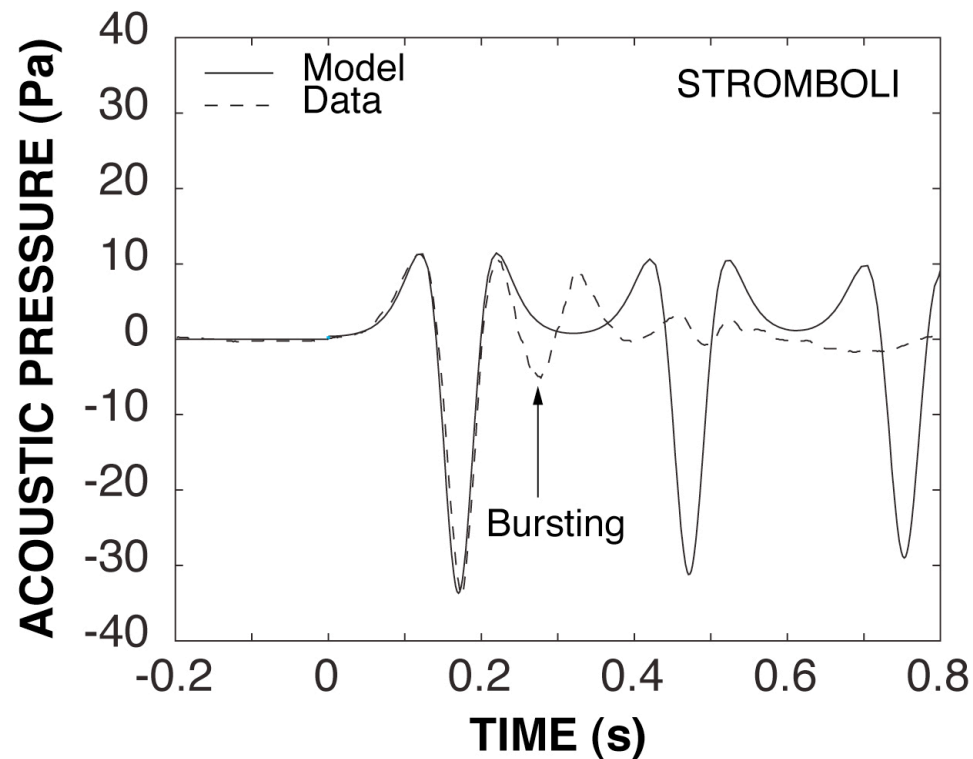


Bubble grows and pass equilibrium position with non-zero velocity:
bubble overshoot, so the bubble become larger than equilibrium
has a pressure less than equilibrium. Gas compressibility acts to
restore the equilibrium pressure, so bubble shrinks.

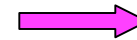
➡ bubble oscillations

Direct measurements (15): Acoustic records

Bubble vibration model:
comparison between theory and
measurements: best fit method



Bubble bursting at the
surface of lava lake (Kilauea)

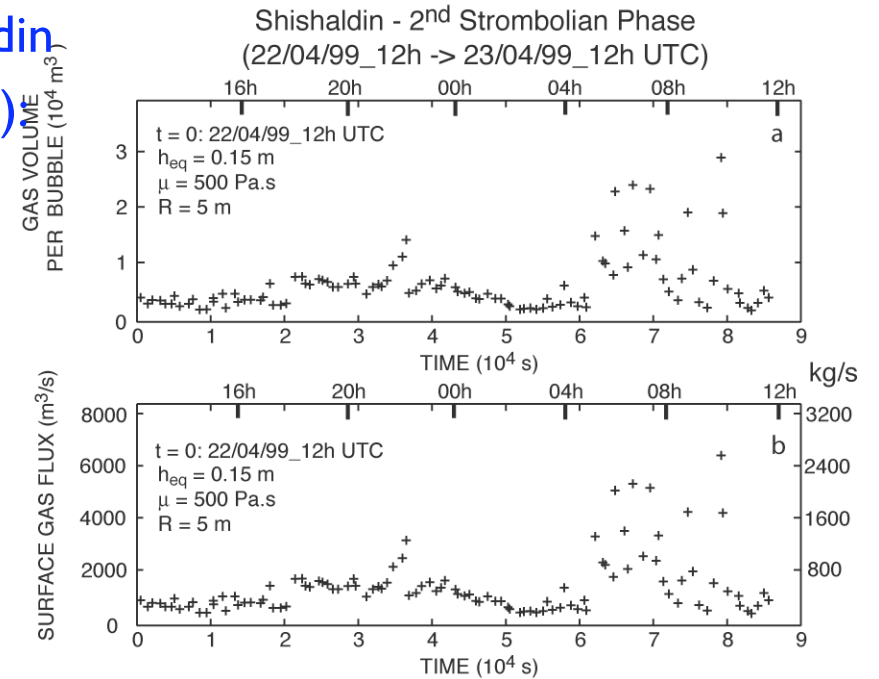
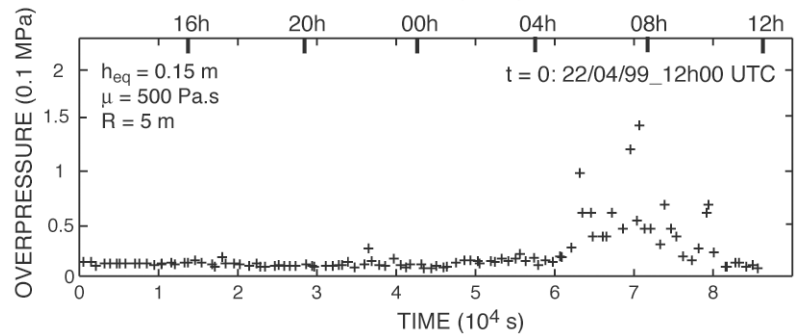
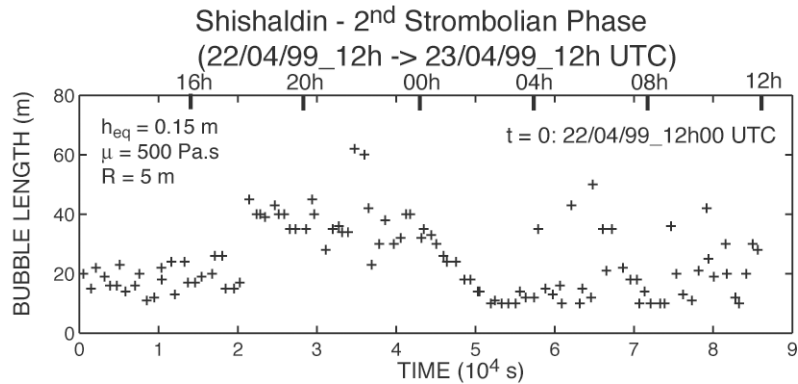


Model for source of sound:
bubble radius, length,
overpressure
and their evolution in time

Model is very robust for gas volume estimates
because it is based on frequency content

Direct measurements (I 6): Acoustic records

Shishaldin
(Alaska)



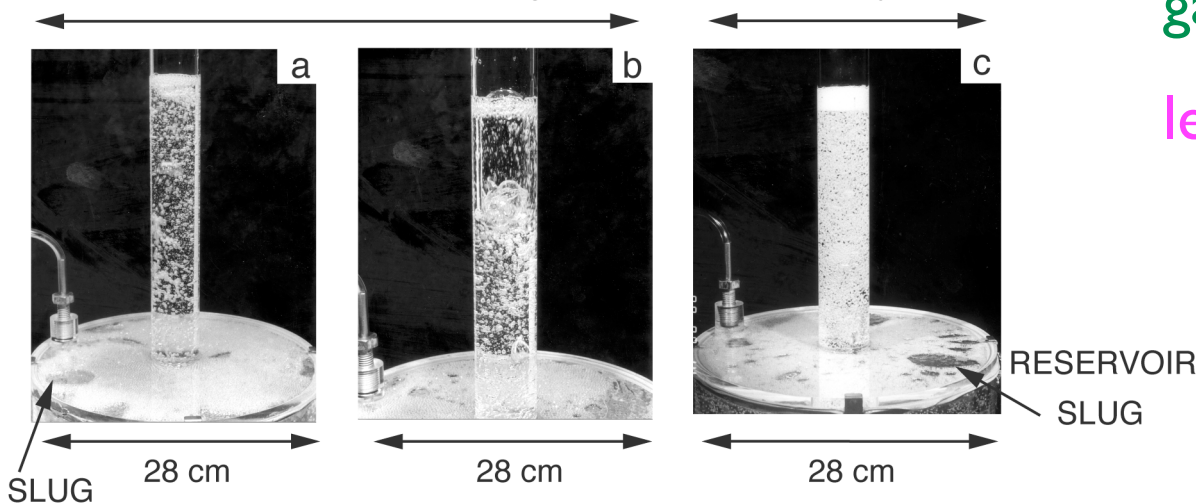
bubble length, pressure,
gas volume and gas flux

length > 2 radius

slug flow

Peak in pressure: rise of
large bubbles in a very
bubbly magma

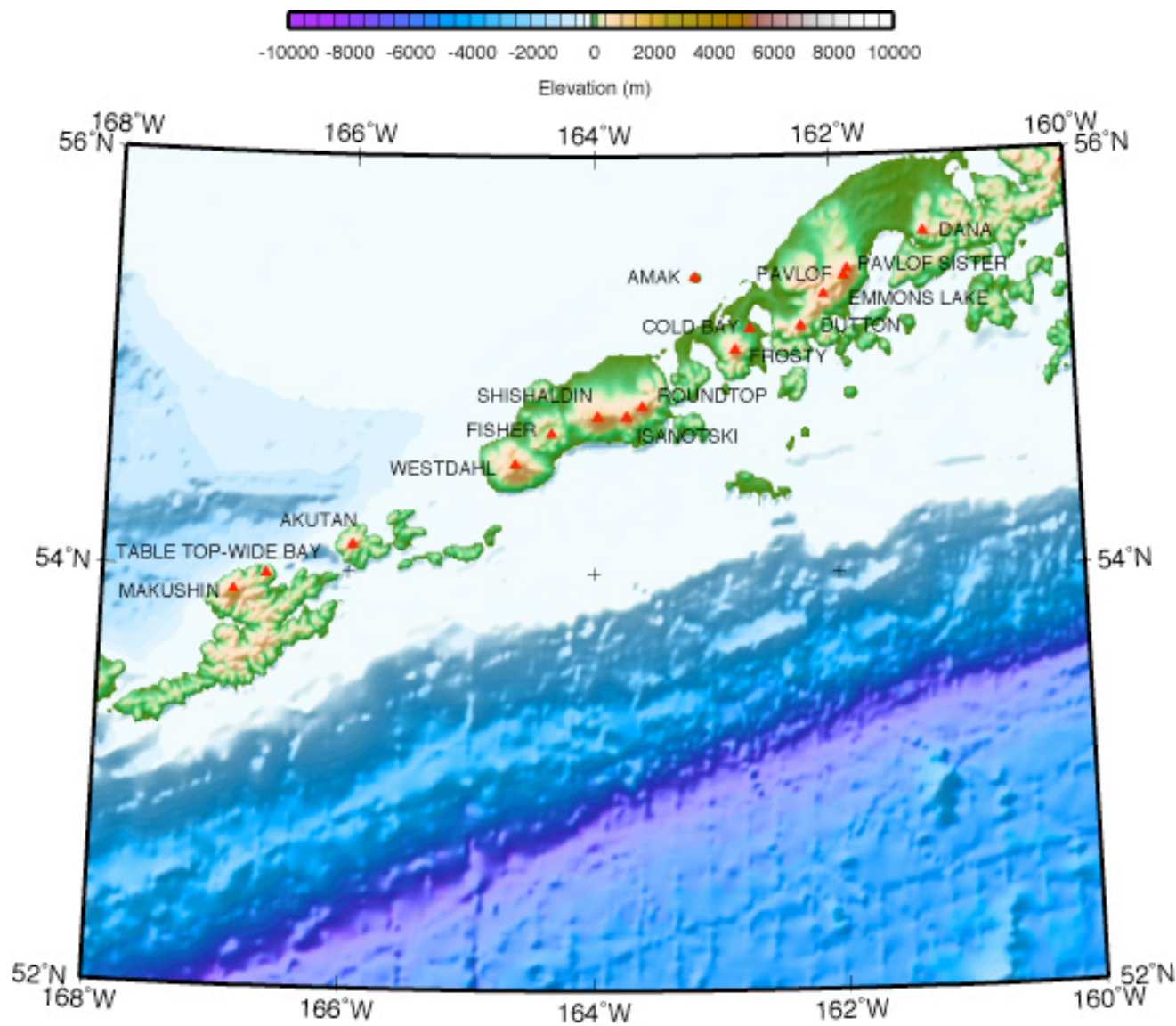
1999 Shishaldin Eruption: 2nd Strombolian Phase
Classical Strombolian activity Peak in overpressure



Direct measurements (17): Acoustic records

The 1999 Shishaldin eruption

Alaska subduction zone



Shishaldin

trench

Direct measurements (18): Acoustic records

Shishaldin,
Alaska, USA

Formation of a basaltic plume
height > 16 km

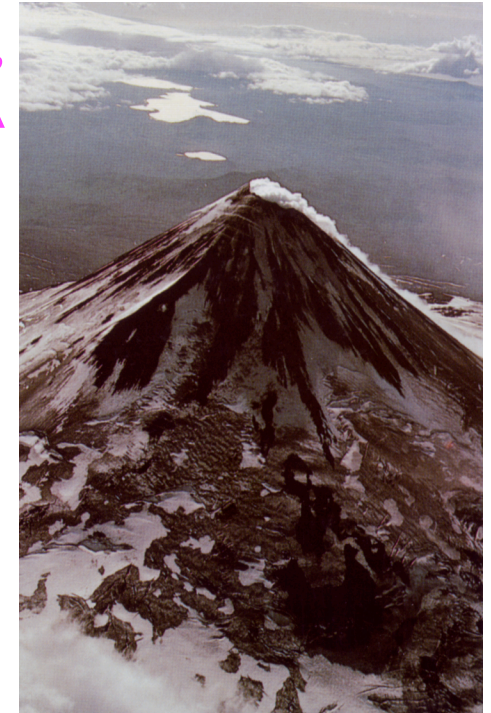
30 % of volcanoes in subduction
zone are basaltic (basaltic andesite)

Basaltic plume is very rare

Eruption finishes with Strombolian activity
(a series of large bubbles breaking)

Plume = very analogous to explosive eruptions

Acoustic measurements
origin of basaltic Subplinian activity
transition Subplinian- Strombolian



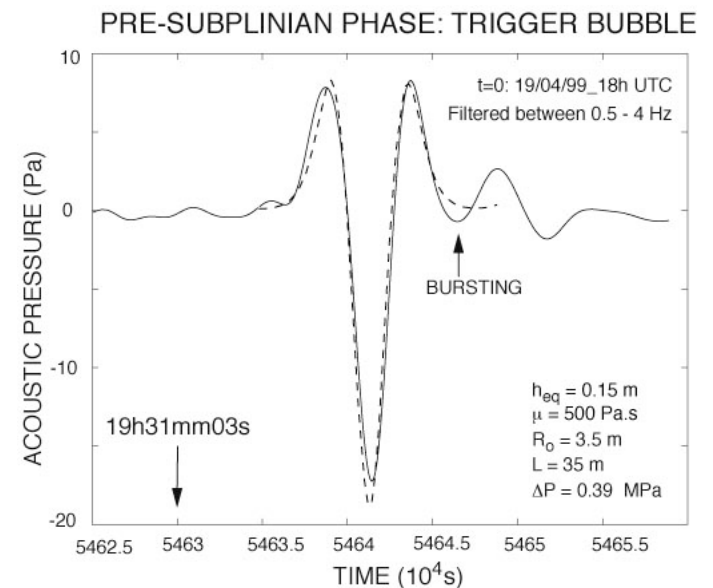
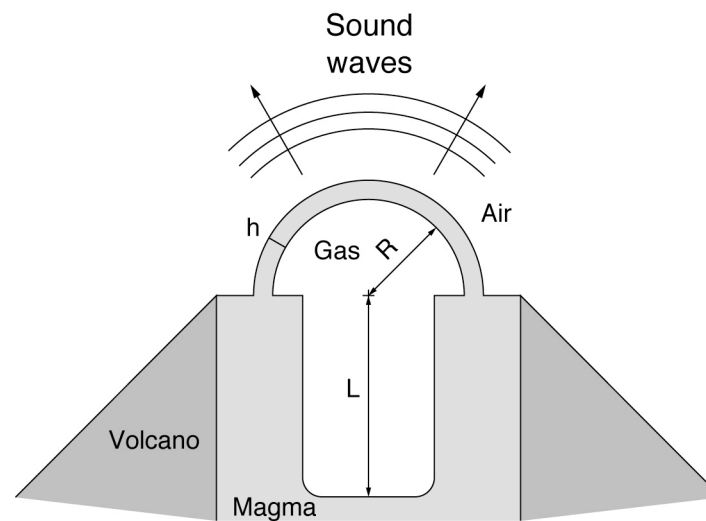
Shishaldin 23/04/99



Direct measurements (19): Acoustic records

Transition to the Subplinian phase:

Very different acoustic pressure than during plume: identical to a single strombolian explosion = bursting of a large overpressurised bubble formed at the depth of the reservoir



Model of bubble vibration:

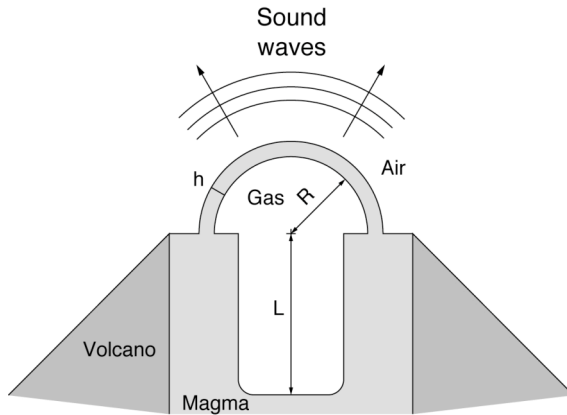


$L = 35$ m; $\Delta P = 0.39$ MPa

Direct measurements (20): Acoustic records

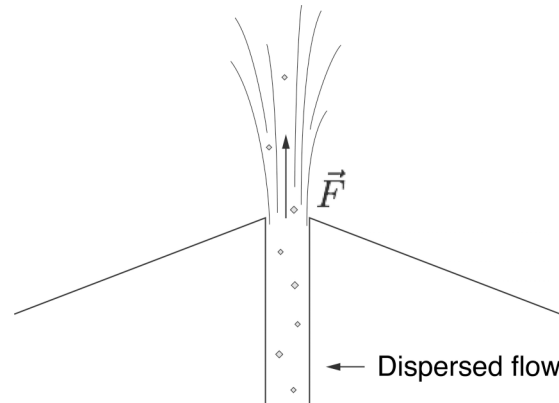
Different types for source of sound:

monopole source



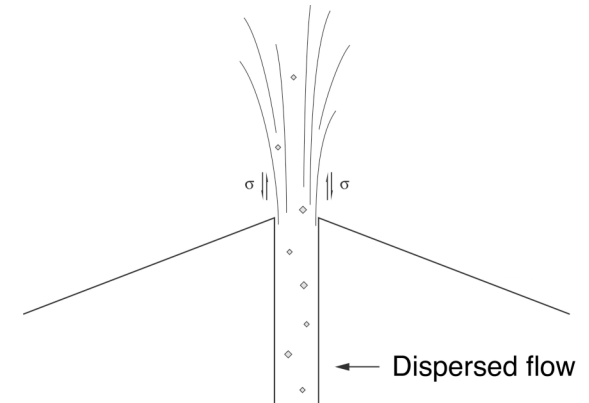
variation of mass flux

dipole source



+ variation of external force (walls of conduit)

quadrupole



+ variation of stress (turbulence)

Acoustic power Π_m is proportional to $(U: \text{gas velocity})^n$

$$\Pi_m = K_m \frac{4\pi R_b^2 \rho_{\text{air}} U^4}{c}$$

$K_m = 1$ (sphere)
(1/16 flat circular)

$$\Pi_d = \frac{K_d \rho_{\text{air}} A_d U^6}{c^3}$$

$K_d = 1/3$
(or 0.013)

$$\Pi_q = \frac{K_q \rho_{\text{air}} \pi R_c^2 U^8}{c^5}$$

$K_q = 3 \cdot 10^{-5} - 10^{-4}$

K_m : empirical constant; R_b and R_c : bubble and conduit radius; c : sound speed

Direct measurements (21): Acoustic records

Subplinian phase:

Complex waveform



use of acoustic power Π_d :
proportional to gas velocity

$$\Pi = \frac{\pi r^2}{\rho_{\text{air}} c T} \int_0^T |p_{\text{ac}} - p_{\text{air}}|^2 dt$$

$$\Pi_d = \frac{K_d \rho_{\text{air}} A_d U^6}{c^3} \quad K_d = 1/3$$

6 periods

gas flux = velocity x area

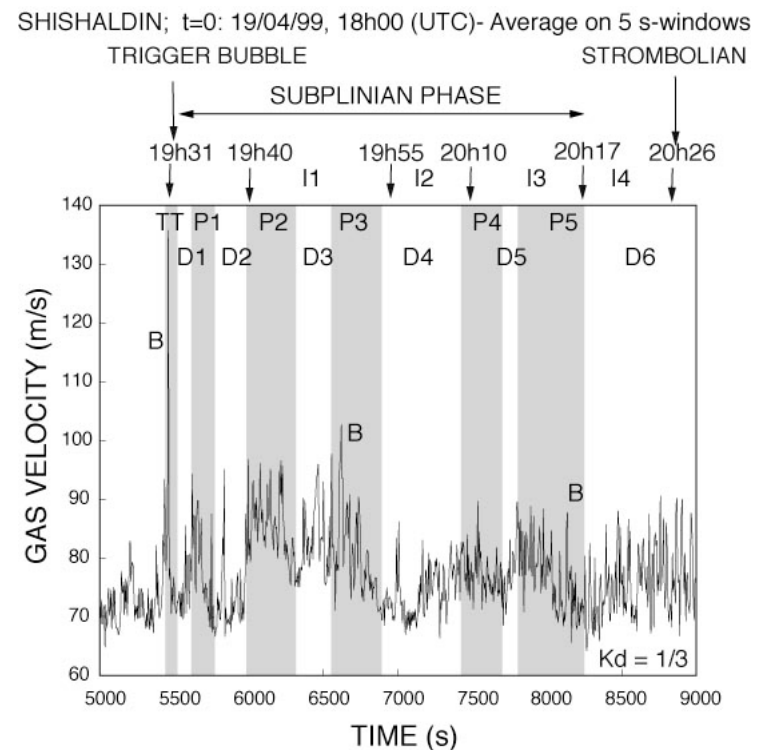
In very good agreement with the gas flux deduced
from the height in the atmosphere

gas flux = gas volume/time



gas volume = $1.5 \cdot 10^7 \text{ m}^3$

Shishaldin
23/04/99



Direct measurements (22): Acoustic records

Other basaltic volcanoes have magmatic plume eruptions:



Cerro Negro
(Nicaragua)



Lopevi
(Vanuatu)

1992, similar to 1968 eruption
(6 wt% H_2O + 1 wt% CO_2);

10 km high plume
(2001, 2003, next?)

Similar mechanisms than Shishaldin?

Basaltic magma reservoirs

1. Physical parameters
2. A laboratory volcano:
3. Gas volume measurements

4. Conclusion

Velocity measurements
with a Sodar at
Stromboli, juin 1991



Conclusion (I):

Hawaiian eruption: cyclicity between fire fountains and effusive activity



Fire fountains (Puu
O'o eruption)

Lava flow into sea
(Kilauea, March 1988)



Cyclicity is related to the degassing
reservoir: formation of a foam at
the top of the reservoir

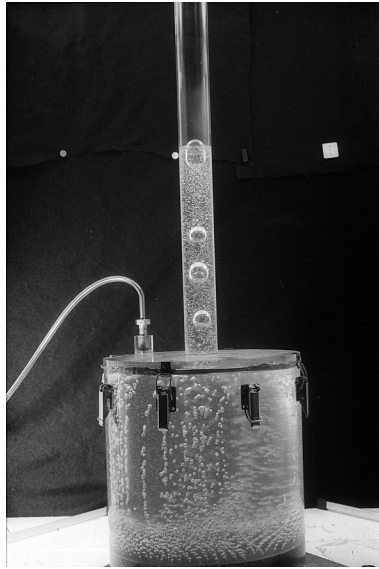


bubble diameter in
reservoir = 0.4 mm

Eruption stops when magma chamber does not contain much bubbles

Conclusion (2):

Strombolian eruption: a series of explosions

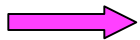


Bubble bursting
at Etna, July 2001

Alternance between gas pockets and no activity: is similar to Hawaii but corresponds to a larger magma viscosity

Etna: cyclic fire fountains + gas composition gives unambiguous evidence for being driven by gas accumulation at depth

Eruption dynamics is driven by gas



Need for measurements of gas volume
such as radar and acoustic measurements, ...